

Ionospheric slab thickness – Analysis, modelling and monitoring

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Abstract

A review of the climatological and storm-time behaviour of the ionospheric slab thickness is presented based on long-time observations at a European mid-latitude site, Dourbes (50.1°N, 04.6°E), and on published results from other studies. An operational electron density and slab thickness monitoring system, established to provide real-time characterisation of the local ionospheric dynamics, is outlined together with some exemplary results.

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1. Introduction

The ionospheric slab thickness (τ) is defined (Davies, 1990) as the ratio of the Total Electron Content (TEC) to the maximum ionospheric F2-layer electron density (NmF2), or in terms of the F2 critical frequency (foF2), $\tau = \text{TEC}/(1.24 \times 10^{-6}(\text{foF2})^2)$, where TEC is measured in TECU (1 TECU = 10^{16} electrons per square metre), foF2 in MHz, and τ in metres. In other words, τ represents the equivalent slab thickness/depth of an idealised ionosphere which has the same electron content as the actual ionosphere but uniform electron density equal to the maximum electron density (Fig. 1). Strictly speaking, when TEC is obtained by means of GNSS (Global Navigation Satellite System) signals, the slab thickness value will contain a plasmaspheric component in addition to the ‘pure’ ionospheric component (Breed et al., 1997). Slab thickness measurements offer substantial information on the shape of the electron density profile, the neutral and ionospheric temperatures/gradients, on the ionospheric composition and dynamics (Titheridge, 1964; Amayenc et al., 1971; Titheridge, 1973; Fox et al., 1990; Davies and Liu, 1991).

Various studies indicated the close relationship between the ionospheric slab thickness and the vertical scale height (e.g. Wright, 1960; Furman and Prasad, 1973; Stankov and Jakowski, 2006). The plasma scale height is defined (Davies, 1990; Hargreaves, 1992) as $H_p = kT_p/m_i g$, where m_i is the ion mass, $T_p = T_i + T_e$ is the plasma temperature, T_i and T_e – ion and electron temperatures, k – the Boltzmann constant (1.380658×10^{-23} J/deg). Similarly, the scale height can be defined for each ion or neutral constituent (Van Zandt, 1967). Practically, the vertical scale height can be approximately deduced by measuring the vertical distance in which the concentration changes by a factor of an exponent (Fig. 1).

Long-time observations have already proved that the slab thickness is subjected to substantial diurnal, annual, latitudinal and storm-time variations, and is influenced (albeit to a lesser extent) by solar and geomagnetic activity (Titheridge, 1973; Furman and Prasad, 1973; Kersley and Hajeb-Hosseinieh, 1976; Bhuyan and Tyagi, 1987; Davies and Liu, 1991; Buonsanto, 1999; Jayachandran et al., 2004). Although the τ irregular behaviour has been studied to some extent (e.g. Titheridge and Andrews, 1967; Kersley and Hajeb-Hosseinieh, 1976; Buonsanto et al., 1979; Fox et al., 1990; Jayachandran et al., 2004; Gulyaeva and Stanislawska; 2005), more investigations are needed in order to better understand and model short-term,

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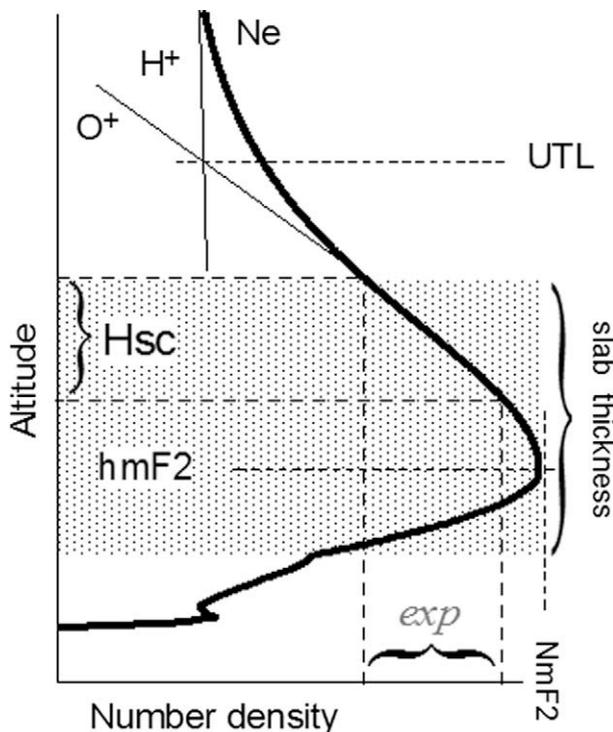


Fig. 1. Schematic view of the vertical electron density profile with key characteristics such as the peak density ($NmF2$), peak height ($hmF2$), upper ion transition level (UTL), scale height (Hsc) and slab thickness (τ).

day-to-day and storm-time changes (Leitinger et al., 2004; Kouris et al., 2004).

This paper presents an overview of the climatological and storm-time behaviour of the slab thickness. In both cases, observations at a European mid-latitude site, Dourbes (coordinates: 50.1°N, 4.6°E (geographic), 51.7°N, 88.9°E (magnetic)), will be used. Modelling and monitoring efforts are discussed and details of a local ionospheric electron density/slab thickness monitoring system will be presented together with results from recent interoperability test.

2. Measurements

The Royal Meteorological Institute (RMI) Geophysics Centre at Dourbes is a complex observational site where meteorological, ionosphere sounding, geomagnetic, TEC and other measurements have been regularly carried out for many years. The Dourbes ionosonde (URSI code: DB049) carries out regular vertical incidence soundings with a Digisonde 256 developed by the University of Massachusetts – Lowell (Reinisch, 1996). Although the ionograms are automatically scaled, manually corrected hourly values of f_oF_2 are used here for more accurate results. TEC observations have been made with a GPS (Global Positioning System) receiver, collocated with the ionospheric sounder, applying a computational procedure based on the ‘geometry-free’ combination of the GPS code and phase measurements for resolving the ambiguities

(Warnant, 1997, 1998; Warnant and Pottiaux, 2000). Receiver and satellite group delays are estimated by modelling the slant TEC with a simple polynomial depending on latitude and local time. The conversion to vertical TEC is performed by assuming the standard ionospheric thin-shell model at a mean ionospheric height of 350 km (e.g. Hofmann-Wellenhof et al., 2008). To obtain a TEC value representative of the ionosphere above a given location, selected and averaged are all values within a latitudinal range of $\pm 1.5^\circ$ over a 15 min period. The slab thickness database consists of measurements since July 1994, i.e. covering more than one complete solar cycle period. For the analysis, the data has been sorted according to season, solar and geomagnetic activity. Thus, measurements from July 1994 to December 1997 were selected to represent low solar activity (LSA) conditions and measurements from July 1999 to December 2002 for high solar activity (HSA). Also, ‘low’ magnetic activity (LMA) conditions are considered when $Kp < 3$, and active, ‘high’ magnetic activity (HMA) – when $Kp \geq 3$. Three seasons (winter, equinox and summer) have been defined as 91-day periods centred on the corresponding winter solstice (day of year, DoY, 356), summer solstice (DoY 173) and equinoxes (DoY 81 and DoY 264).

3. Climatological behaviour

Based on long-time series of f_oF_2 and TEC data, numerous analyses have been published on the climatological behaviour of the slab thickness. As mentioned in Section 1, it has been found that the slab thickness shows diurnal, seasonal, spatial, solar and geomagnetic activity variations. Specific features were revealed, such as the pre-dawn (PDE) enhancement and the correlation with the plasma scale height behaviour.

The mean diurnal variations of the slab thickness observed at Dourbes (Fig. 2) are characterised with night-time values that are substantially higher than the day-time values during winter (night-to-day ratio between 1.40 at HSA and 1.55 at LSA), but higher day-time and lower night-time values during summer (night-to-day ratio of 0.80 HSA to 0.86 LSA). A pre-dawn increase of the slab thickness is observed in the winter and equinox seasons, most pronounced during LSA winter between 05:00LT and 06:00LT, when average values exceed 400 km. On average, the higher solar activity induces higher slab thickness values, both during night (up to 14%) and day (up to 24%). Active geomagnetic conditions also tend to elevate the slab thickness, more noticeably (in percentage terms) at HSA. Most prominent are the seasonal changes. During LSA, the average day-time values increase from 181 km in winter to 316 km in summer, while during HSA, the values almost double from winter (205 km) to summer (390 km). The night-time values however, do not experience such large variability from winter to summer. There is comparatively small diurnal variation in τ during the equinoctial months.

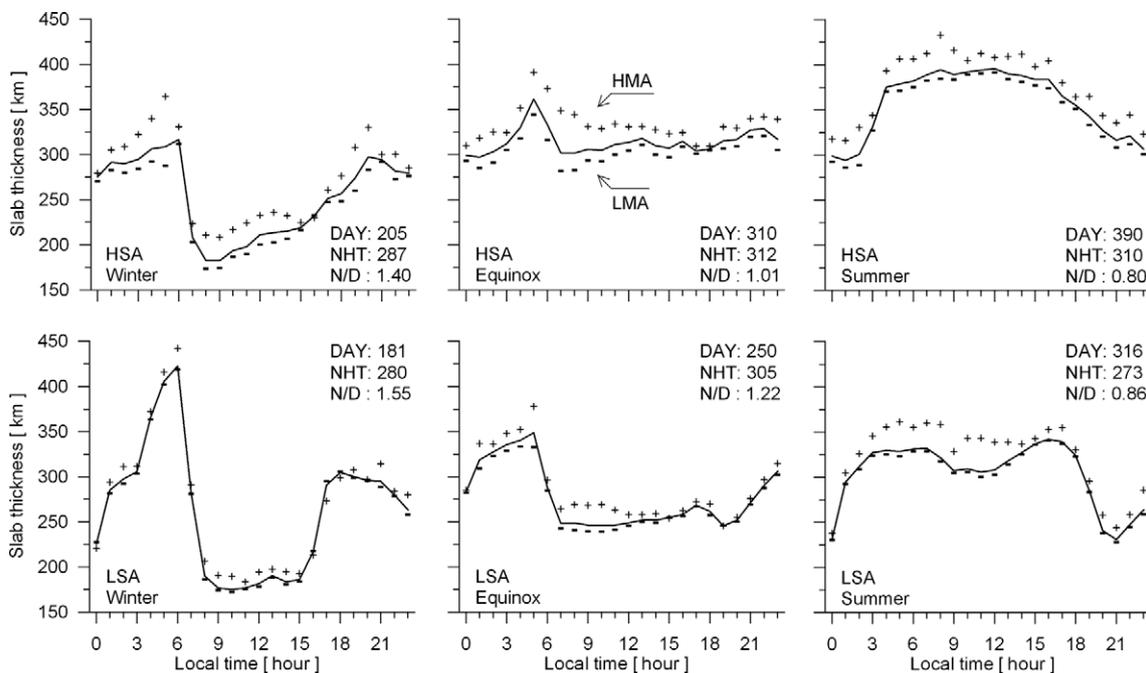


Fig. 2. Diurnal variations of the slab thickness during low (bottom panels) and high (top panels) solar activity, as deduced from measurements at Dourbes (50.1°N, 04.6°E). Solid lines show the average variations based on data from all geomagnetic conditions, the ‘-’ symbols denote the average values observed during low magnetic activity (LMA, $K_p < 3$) and the ‘+’ symbols denote the values during high magnetic activity (HMA, $K_p \geq 3$) conditions.

The slab thickness exhibits a pronounced pre-dawn enhancement (PDE). The pre-dawn increase is a phenomenon closely related to the maintenance of the night-time F layer and can sufficiently well be explained (e.g. Davies and Liu, 1991) by the lowering of the ionospheric F layer immediately before sunrise to regions of greater neutral density, leading to increased ion loss due to recombination. The effect is believed to be particularly strong in the bottom-side ionosphere that includes the density peak. As a result, the decrease in NmF2 and the bottom-side density is much faster than the topside ionosphere where the loss rate is lower and thus, an enhancement occurs. In addition, plasmaspheric fluxes can also play a role in the increase. The magnitude of this increase is reportedly larger in low latitudes than in middle latitudes (Davies and Liu, 1991). By using data from Goose Bay (53.32°N, 299.16°E), Boulder (40.00°N, 254.70°E) and Hawaii (20.80°N, 203.50°E), Jayachandran et al. (2004) report that the PDE is a regular feature appearing during solar minimum in all seasons and latitudes, while during solar maximum it is still preserved for high and low latitudes but not evident at middle latitudes. Indeed, from our observations (Fig. 2) the PDE seems to gradually disappear from winter to summer.

Substantial diurnal and seasonal variability of τ has been recorded during the years. Several studies in the northern hemisphere indicate that, generally, the slab thickness is greater in summer than in winter (Roger, 1964; Spalla and Ciraolo, 1994; Minakoshi and Nishimuta, 1994; Leitinger et al., 2004). Observations from the southern hemisphere confirm that the day-time slab thickness is greater in summer than in winter (Titheridge, 1973; Good-

win et al., 1995; Breed et al., 1997). Nevertheless, there are obviously some differences. For example, Jin et al. (2007) report that, in the East Asian zone, larger day-time values are maintained during equinox while smaller values are observed in summer and winter. Moreover, two peaks appear around 10:00 LT and 18:00 LT, most distinctively in summer.

Concerning the solar activity influence, Davies and Liu (1991) in a study based on measurements from globally distributed stations have found that the slab thickness varies linearly with the 12-month smoothed values of the 10.7-cm solar radio flux. However, in middle latitudes they observed that, while the mid-day slab thickness increases in line with the solar flux during all seasons, the midnight slab thickness is essentially independent of the solar flux. It was also reported by Jayachandran et al. (2004) that, at higher latitudes, the slab thickness does not change significantly during low solar activity but, at higher solar activity, it increases in step with the increasing solar flux values. At lower latitudes, the mean day-time values remain more or less constant for both low and high solar activity. For the equatorial region, Klobuchar et al. (1991) calculated a slab thickness peak of about 510 km during solar maximum conditions and, during solar minimum conditions, a corresponding peak in the range of 460–560 km depending on the drift conditions. Also, at low and equatorial latitudes, the median day-time value of the slab thickness seems to be poorly correlated with the solar activity index $F_{10.7}$ (Chuo, 2007). In Australia, Breed et al. (1997) observed even a trend for increased slab thickness values at times of reduced solar influence. The

PDE is reported to be well pronounced during the solar minimum, gradually disappearing during the ascending part of the solar cycle, and reappearing during the solar maximum, particularly in winter (Minakoshi and Nishimuta, 1994).

Although the magnetic activity does not appear to have significant influence on the τ variations at equatorial and low latitudes (Jayachandran et al., 2004; Chuo, 2007), active magnetic conditions seem to enhance the τ values at middle latitudes during solar minimum and at high latitudes during solar maximum (Buonsanto et al., 1979). A positive correlation has been detected between the monthly mean values of the slab thickness and the Ap geomagnetic index (Kersley and Hajeb-Hosseini, 1976), explained with the dependence of the neutral gas temperature on the level of magnetic disturbances. Fox et al. (1991) argue that while a correlation with daily magnetic indices can be expected, correlation with monthly mean magnetic activity is not justified.

There are no clear-cut trends established in the spatial variations of the slab thickness. For example, Buonsanto et al. (1979) observed that the slab thickness is nearly always smaller at middle latitudes than at sub-auroral latitudes, while Klobuchar et al. (1991) found a region of enhanced slab thickness, extending from equatorial to dip latitudes of around $\pm 34^\circ$. Leitinger et al. (2004) conclude from theoretical considerations that there is an increase in the slab thickness towards the dip equator when the equatorial anomaly is on. Jayachandran et al. (2004) report (from northern hemispheric observations) that, during night, highest average values of τ (and night-to-day ratios) are recorded at high latitudes during solar maximum and at middle latitudes during solar minimum. Reported observations from the southern hemisphere do not indicate a noticeable latitudinal dependence in any season (Goodwin et al., 1995). By combining vertical electron content (derived by means of the Faraday effect on VHF signals from geostationary satellites) with peak electron density (derived from ionograms), and after neglecting solar activity, diurnal and seasonal variations, Leitinger et al. (2004) estimated that the overall mean slab thickness for Europe can be given as 230 km with a standard deviation of 50 km. For high solar activity however, an increased aver-

age around 300 km is found to be more appropriate. The overall means for the American sector are slightly higher: $\tau = 242$ km for low solar activity, $\tau = 267$ km for moderate solar activity and $\tau = 292$ km for high solar activity (Fox et al., 1991).

The average behaviours of the slab thickness and the topside ionospheric scale height seem to correlate well (cf. Figs. 2 and 3), due to the fact that most of the mechanisms determining the plasma scale height are valid for the slab thickness behaviour as well (Stankov et al., 2007). Here, the topside scale height value (at ~ 425 km altitude) is obtained directly from the vertical electron density profile retrieved from ionospheric radio occultation measurements (Stankov and Jakowski, 2006). However, such correlation is not obvious under disturbed conditions when compression/expansion of the electron density profile is controlled mainly by dynamic forces such as neutral winds and electric fields.

4. Storm-time behaviour

The greatest variability in ionospheric slab thickness is observed during periods of geomagnetic storms. Here, we present the slab thickness perturbations during two storm events, the summer storm of 15 July 2000 and the winter storm of 7 November 2004 (Fig. 4).

The July 2000 storm was classified as a severe storm (Dst index fell to -300 nT) which induced substantial negative response by both, foF2 and TEC, most pronounced during the main and early recovery phases (from 14:35UT on 15 July 2000 until about 09:00UT on 16 July 2000) when the foF2 and TEC percentage deviations from monthly means dropped below -50% and -80% , respectively (Fig. 4, left panels). In fact, neither foF2 nor TEC experienced a 'positive' phase and were not able to recover to their normal values until 17 July. There is no foF2 data around 00:00UT on 16 July, so the slab thickness was not possible to calculate, but judging from the neighbouring values, it is obvious that the largest increase in the slab thickness occurred during the evening of 15 July and the early hours of 16 July when the slab thickness exceeded 600 km. Increased slab thickness values were actually observed for most of the storm period.

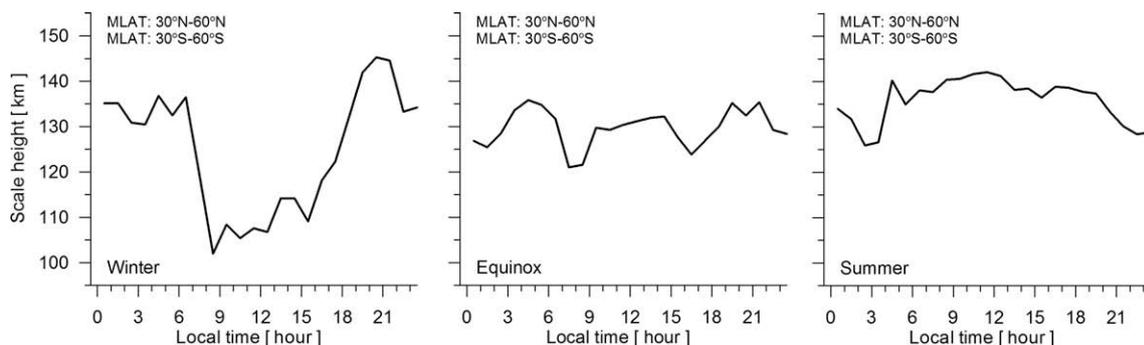


Fig. 3. The topside ionospheric scale height, deduced from ionospheric occultation measurements (Stankov and Jakowski, 2006), middle geomagnetic latitudes (MLAT) during winter, equinox and summer.

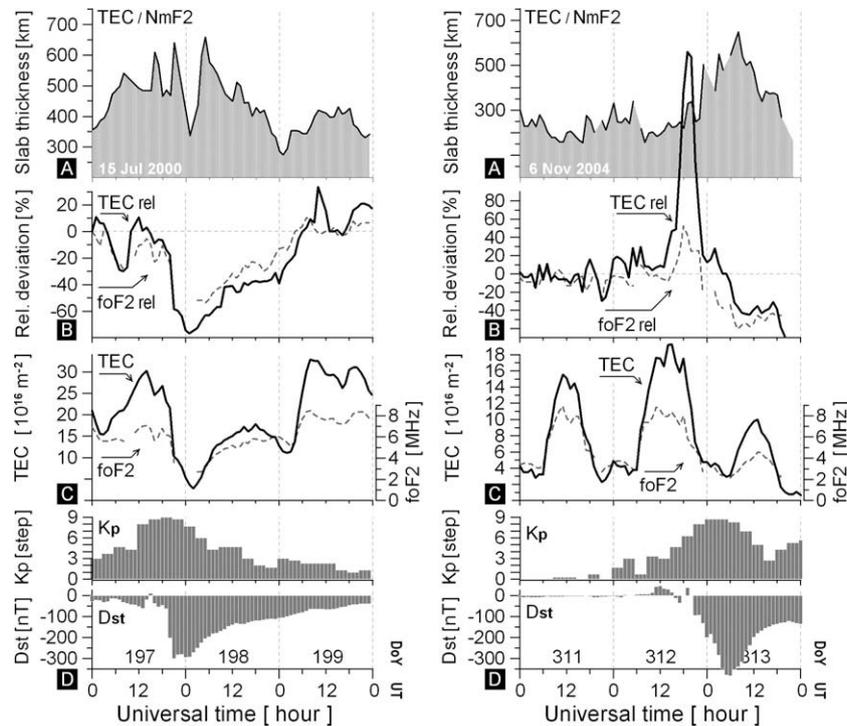


Fig. 4. The slab thickness behaviour (top panels) during the geomagnetic storm periods of 15–17 July 2000 (left panels) and 6–8 November 2004 (right panels) as observed at Dourbes (50.1°N, 04.6°E).

The 7 November 2004 event was even more severe (Dst plunged to almost -400 nT) and longer lasting. It was characterised by a pronounced positive response from both the foF2 and TEC parameters during the onset phase of the storm, with percentage deviations from monthly means increasing above 50% for foF2 and more than 200% for TEC (Fig. 4, right panels). As a result, the slab thickness also increased substantially to peak at almost 650 km (in excess of 250% above the monthly means) during the early stages of the storm recovery phase when foF2 was much more seriously depressed than TEC. The slab thickness remained higher than the monthly means until the evening hours of 8 November. In a previous study of the same storm with data from Juliusruh (54.6°N, 13.4°E), a similar pattern of behaviour was observed (Stankov et al., 2005).

Key factors affecting the storm-time perturbations of the slab thickness are the levels of the solar and geomagnetic activity, the season, and the storm onset time, among others. In an extensive study, Fox et al. (1990) analyse in great detail the average storm patterns of the slab thickness behaviour by using a database of two solar cycles of TEC observations from Hamilton, MA (42°N, 288°E) and ionosonde observations from Wallops Island, VA (37.8°N, 284.5°E). The first noticeable feature is that the slab thickness is systematically enhanced during periods of geomagnetic disturbances, both during the positive and negative phases of TEC and NmF2. Although the duration of the average storm effect does not seem to be seasonally dependent, it appears that the enhancement on the first day of the storm is greater in winter, while that

observed on the second day of the storm is greater in summer. The intensity of the storm proved important – the relative enhancements in τ are clearly greater during storms corresponding to greater peak Ap index values. While no dramatic trend is visible as a result of varying the level of solar activity, the effect on the slab thickness is greater during periods of higher solar activity. Significant differences in the τ storm patterns were detected with respect to the storm onset time. Thus, when onset occurs early in local time, a substantial increase is seen on the first day of the storm and a reduced effect on the second day. The enhancement tends to be greater for mid-day onsets and the effect lasts longer if the onset occurs later in the day.

Other researchers also noted that, if the sudden storm commencement occurs during day-time in winter, then a positive phase in the slab thickness is observed for the rest of the day followed by a negative phase the next day, whereas in summer, the slab thickness shows a positive phase during the entire storm period (Titheridge and Andrews, 1967; Mendillo, 1973). Prolonged slab thickness enhancements, lasting up to 48 h after the storm onset, have been seen during the negative storm phases of NmF2 and TEC during solar maximum, while during solar minimum the enhancement may be significantly delayed (up to 24 h after the storm onset) (Gulyaeva and Stanislawska, 2005). Theoretically, an increasing slab thickness (e.g. rising TEC accompanied by constant or decreasing foF2) indicates plasma uplifting – a manifestation of active electric fields that produce a vertical drift driving the plasma upwards to regions of lower ion loss (Buonsanto,

1999). At high/auroral latitudes, slab thickness increases may be attributed to heating processes leading to higher plasma temperatures, and additionally, at night, to the presence of an auroral E-layer (Buonsanto et al., 1979).

It is obvious that the reliable description and modelling of the day-to-day variations of the ionospheric slab thickness is a challenging task that should focus on long-term monitoring and analysing observations from many storm periods.

5. Modelling efforts

In principle, the slab thickness values can be deduced from ionospheric models (empirical or otherwise) capable of providing vertical electron density profiles, so the focus was on improving the existing ionospheric models rather than developing a stand-alone model of the slab thickness on a global scale.

Nevertheless, there exists a number of local/regional models (e.g. Titheridge, 1973; Hajeb-Hosseinih and Kersley, 1975; Huang, 1983; Fox et al., 1991; Davies and Liu, 1991; Spalla and Ciraolo, 1994). As summarised by Leitinger et al. (2004), these models provide a slab thickness value in the range between 170 and 320 km for low solar activity and between 200 and 400 km for high solar activity, an increase in slab thickness with solar activity, and a slight positive dependence on geomagnetic activity for non-storm conditions. For strong magnetic storm conditions, only a slight day-time increase of 10–30 km is envisaged.

Fox et al. (1991) developed a mid-latitude model for the mean slab thickness values based on Fourier analysis applied to the Hamilton/Wallops Island database and compared the results with ionospheric models available at that time, including the International Reference Ionosphere (IRI). None of the models tested had values that were strong functions of latitude or longitude, so the comparisons were deemed equally valid for other mid-latitude locations. These comparisons yielded substantial discrepancies between the models' output and it was realised that more research relying on modern observation techniques is needed for successful modelling purposes.

A recent development, closely related to the slab thickness modelling efforts, is the global space-time empirical model of the topside 'half-peak density height' (Gulyaeva, 2003; Gulyaeva and Titheridge, 2006). Similar to the sub-peak semi-thickness characteristic of the bottom-side electron density profile (Titheridge, 1973), the topside half-peak density height ($h05_{top}$) is specified as the height in the topside ionosphere where the electron density is half the peak density NmF2. In fact, this global empirical model provides the ratio $Rh05 = (h05_{top} - hmF2)/hmF2$ of the topside half-width to the F-layer peak height, parameterised with respect to solar activity, local time and geomagnetic latitude. The model database is constructed from topside sounding measurements carried out onboard the satellites ISIS1 (1969–1971, orbit altitude 500–3500 km), ISIS2

(1971–1980, altitude 1400 km) and Interkosmos 19 (1979–1982, altitude 500–1000 km), thus covering more than one complete solar activity cycle, including the whole range of diurnal, seasonal and spatial variations of the topside electron density profile.

6. Monitoring developments

An operational system for monitoring the local ionospheric density distribution has been established at the RMI Geophysics Centre at Dourbes (Jodogne and Stankov, 2002). The purpose of the LIEDR (Local Ionospheric Electron Density Reconstruction) system is to acquire and process data from simultaneous ground-based GNSS TEC and digital ionosonde measurements, and subsequently to deduce the local vertical electron density profile. LIEDR is primarily designed to operate in real time for service applications, and, if sufficient data from solar and geomagnetic observations are available, to provide short-term forecast as well. For research applications and further development of the system, a post-processing mode of operation is also envisaged.

A key module of the LIEDR system is the vertical electron density profile reconstruction that uses simultaneous digital ionosonde and GNSS measurements, together with empirically-obtained values of the O^+/H^+ ion transition level. The ionosonde measurements are used primarily for obtaining the bottom-side profile, since digital ionosondes permit the reliable deduction of profiles from about 60 km up to hmF2. The topside electron density profile is deduced by employing a suitable ionospheric profiler (Chapman, Epstein, or Exponential) and solving a system of transcendental equations (resulting from the use of the above profilers) to obtain the unknown topside ion scale heights, sufficient to construct a unique electron density profile at the site of the measurements (Stankov and Muh-tarov, 2001; Stankov, 2002; Stankov et al., 2003). Another key module of the LIEDR operational system is the real-time estimation of the ionospheric slab thickness.

To be able to provide forecast, additional information about the current solar and geomagnetic activity is needed. For the purpose, observations available in real time – at the Royal Institute of Meteorology (RMI), the Royal Observatory of Belgium (ROB) and the US National Oceanic and Atmospheric Administration (NOAA) – are used. Recently, a new hybrid model for estimating and predicting the local magnetic index K has been developed (Kutiev et al., 2009). This hybrid model has the advantage of using both, ground-based (geomagnetic field components) and space-based (solar wind parameters) measurements, which results in more reliable estimates of the level of geomagnetic activity – current and future.

LIEDR has been tested on actual measurements and is now operational with the nominal time resolution between two consecutive reconstructions set to 15 min. Short-term TEC and foF2 forecast is envisaged (Stankov et al., 2004)

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